Calculation Policy

At Luddenden CE, we follow a mastery approach in maths. Concepts and calculations begin with concrete manipulatives so children build good understanding of concepts, not just processes and algorithms. When this stage is secure, pictorial representations model the concept before moving on to abstract representations and formal algorithms.

When setting tasks or phrasing questions, problems will be asked in a variety of ways. Examples are given in the, 'conceptual variations', but these in no way represent an exhaustive list. Children will be encouraged to apply what they have learnt in different ways to deepen understanding and develop resilience to unfamiliar situations.

We recognise that bigger numbers or more digits do not necessarily make questions harder, so numbers in questions are chosen carefully, including zero, to increase in complexity rather than simply scale. For example, 1230 + 1126 is a much simpler calculation than 389 + 934 due to exchanging.

Children are encouraged to use correct mathematical language so they are able to discuss their ideas properly and explain their understanding accurately.

This document is separated by operation and year group, however, some children may need to recap from previous years, or a teacher may start a unit of work by recapping the previous year's techniques and concepts, so the year group assigned to a method or concept should not be taken as a rigid rule.

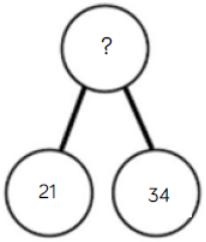
Conceptual Variation

When setting tasks or phrasing questions, problems will be asked in a variety of ways. Children will be encouraged to apply what they have learnt in different ways to develop resilience to unfamiliar situations.

Below is just a sample of ways questions could be phrase or displayed. Teachers will present questions and problems in a broad variety of ways and contexts.

Addition:

Conceptual variation; different ways to ask children to solve 21 + 34



?	
21	34

Word problems:
In year 3, there are 21 children and in year 4, there are 34 children.
How many children in total?

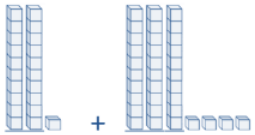
21 + 34 = 55. Prove it

21
+34
——

21 + 34 =

☐ = 21 + 34

Calculate the sum of twenty-one and thirty-four.

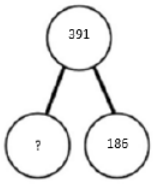


Missing digit problems:

10s	1s
10 10	1
10 10 10	?
?	5

Subtraction:

Conceptual variation; different ways to ask children to solve 391 - 186



391	
186	?

Raj spent £391, Timmy spent £186.
How much more did Raj spend?

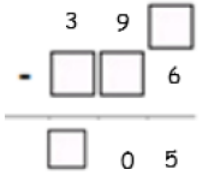
Calculate the difference between 391 and 186.

□ = 391 − 186

391
-186
___

What is 186 less than 391?

Missing digit calculations



Multiplication:

Conceptual variation; different ways to ask children to solve 6 × 23

23	23	23	23	23	23

?

Mai had to swim 23 lengths, 6 times a week.
How many lengths did she swim in one week?

With the counters, prove that 6 x 23 = 138

Find the product of 6 and 23

6 × 23 =

□ = 6 × 23

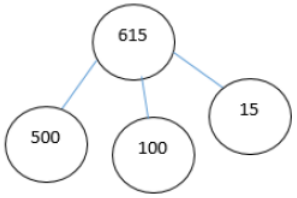
6	23
× 23	× 6
___	___

What is the calculation?
What is the product?

Division:

Conceptual variation; different ways to ask children to solve 615 ÷ 5

Using the part whole model below, how can you divide 615 by 5 without using short division?



I have £615 and share it equally between 5 bank accounts. How much will be in each account?

615 pupils need to be put into 5 groups. How many will be in each group?

$5\overline{)615}$

615 ÷ 5 =

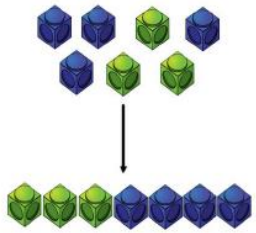
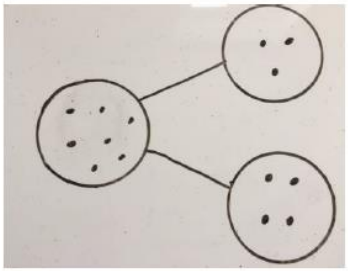
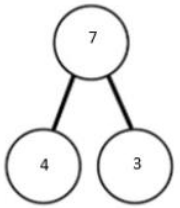
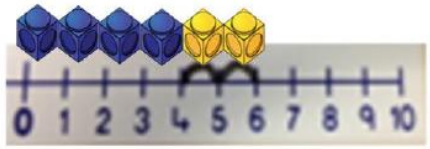
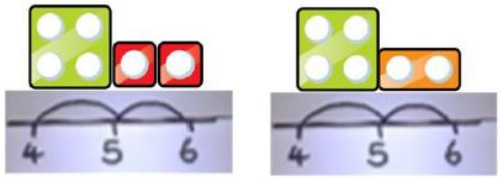
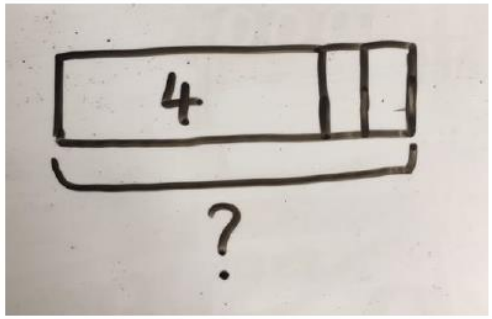
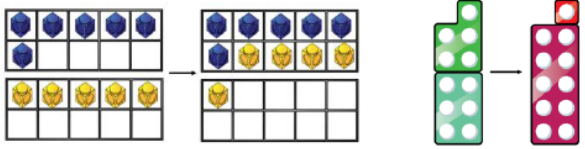
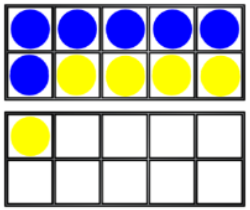
□ = 615 ÷ 5

What is the calculation?
What is the answer?

Year 1

Addition:

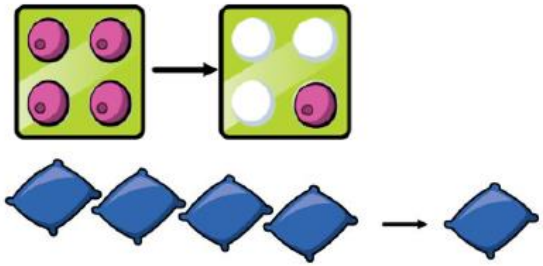
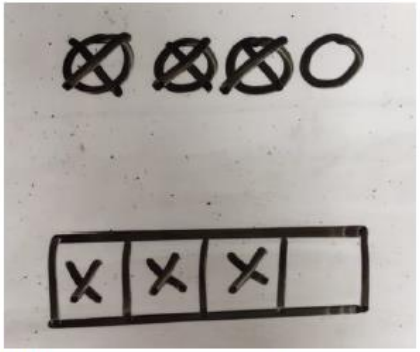
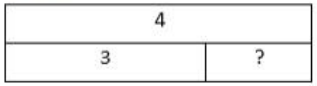
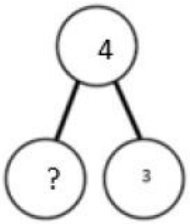
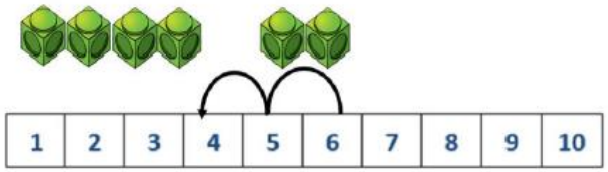
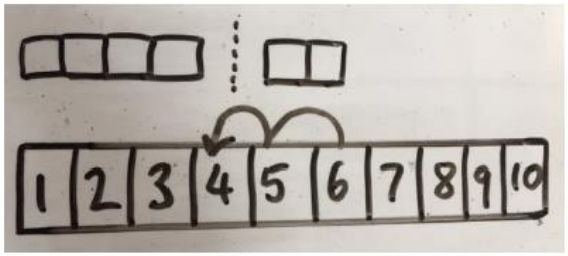
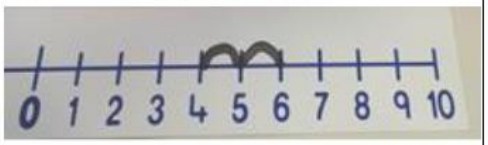
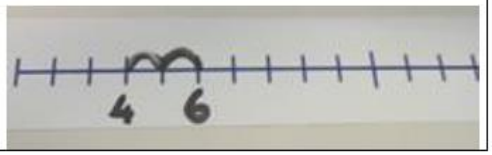
Key Language: Sum, total, parts and whole, plus, add, altogether, more, 'is equal to', 'is the same as'.

Concrete	Pictorial	Abstract
Combining two parts to make a whole (use other resources too e.g. eggs, shells, teddy bears, cars). 	Children to represent the cubes using dots or crosses. They could put each part on a part whole model too. 	4 + 3 = 7 Four is a part, 3 is a part and the whole is seven. 
Counting on using number lines using cubes or Numicon.  	A bar model which encourages the children to count on, rather than count all. 	The abstract number line: What is 2 more than 4? What is the sum of 2 and 4? What is the total of 4 and 2? 4 + 2 
Regrouping to make 10; using ten frames and counters/cubes or using Numicon. 6 + 5 	Children to draw the ten frame and counters/cubes. 	Children to develop an understanding of equality e.g. 6 + □ = 11 6 + 5 = 5 + □ 6 + 5 = □ + 4

Year 1

Subtraction:

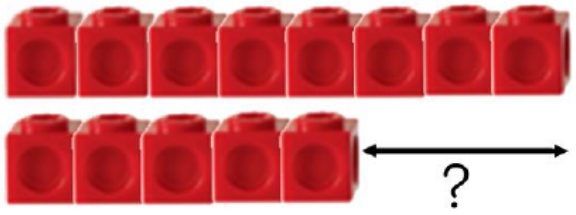
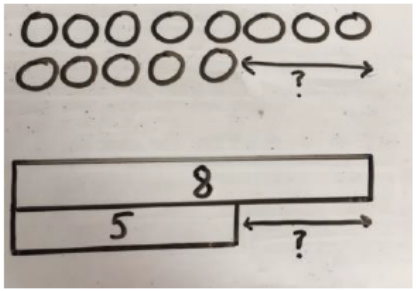
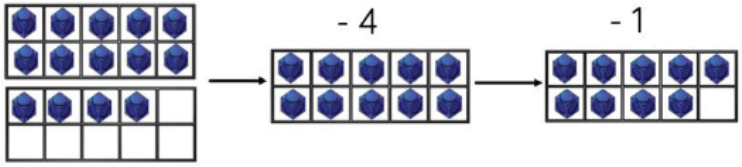
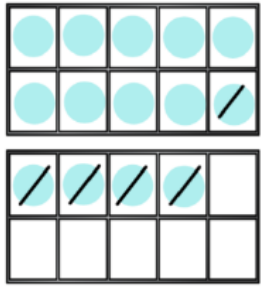
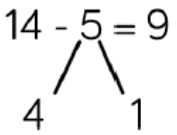
Key Language: Take away, less than, the difference, subtract, minus, fewer, decrease

Concrete	Pictorial	Abstract
Physically taking away and removing objects from a whole (ten frames, Numicon, cubes and other items such as beanbags could be used). 4 – 3 = 1 	Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used. 	4- 3 = □ = 4 – 3  
Counting back (using number lines or number tracks) children start with 6 and count back 2. 6 – 2 = 4  	Children to represent what they see pictorially e.g.  	Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line  

Year 1

Subtraction:

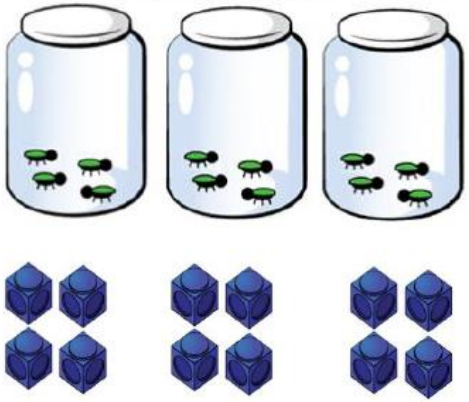
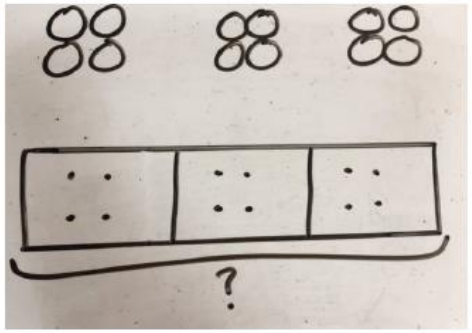
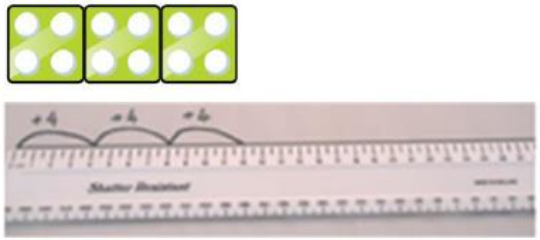
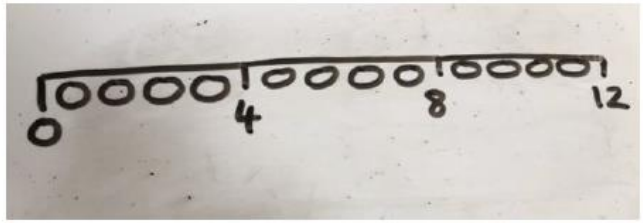
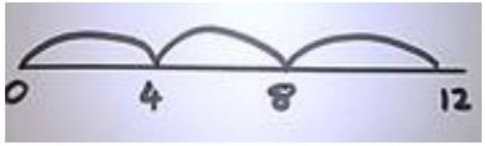
(continued)

Finding the difference (using cubes, Numicon or Cuisenaire rods, other objects can also be used). Calculate the difference between 8 and 5. 	Children to draw the cubes/other concrete objects which they have used or use the bar model to illustrate what they need to calculate. 	Find the difference between 8 and 5. 8 – 5, the difference is ☐ Children to explore why 9 - 6 = 8 – 5 = 7 – 4 have the same difference.
Making 10 using ten frames. 14 – 5 	Children to present the ten frame pictorially and discuss what they did to make 10. 	Children to show how they can make 10 by partitioning the subtrahend.  14 – 4 = 10 10 – 1 = 9

Year 1

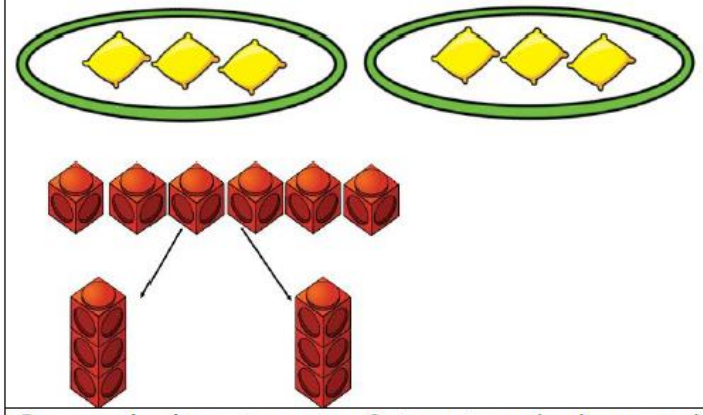
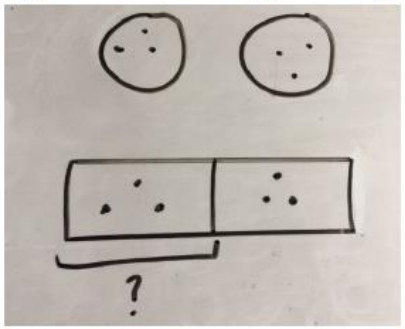
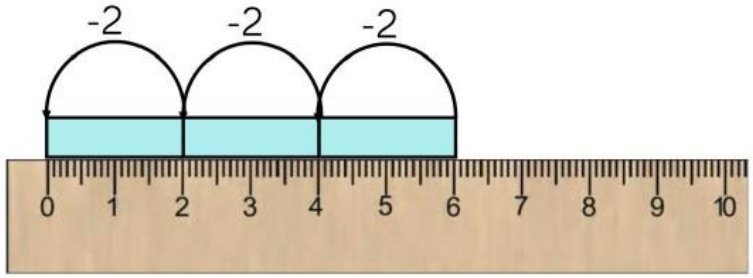
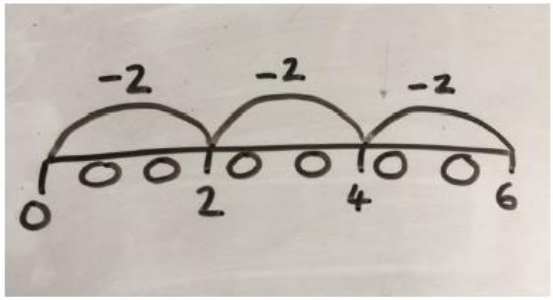
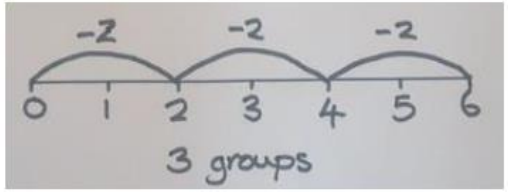
Multiplication:

Key Language: Double, times, multiplied by, the product of, groups of, lots of, equal groups

Concrete	Pictorial	Abstract
Repeated grouping/repeated addition 3 × 4 4 + 4 + 4 There are 3 equal groups, with 4 in each group. 	Children to represent the practical resources in a picture and use a bar model. 	3 × 4 = 12 4 + 4 + 4 = 12
Number lines to show repeated groups- 3 × 4  Cuisenaire rods can be used too.	Represent this pictorially alongside a number line e.g.: 	Abstract number line showing three jumps of four. 3 × 4 = 12 

Year 1 - Division:

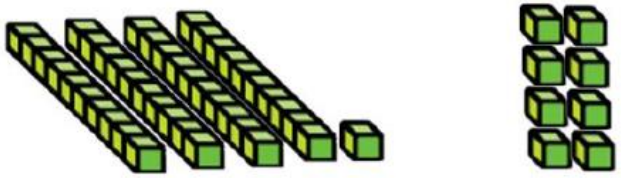
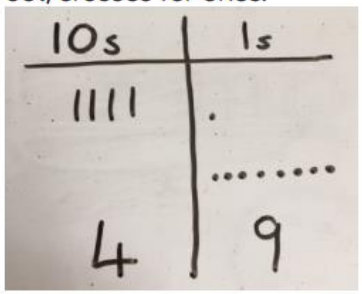
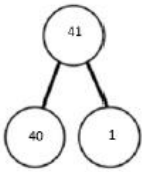
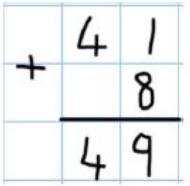
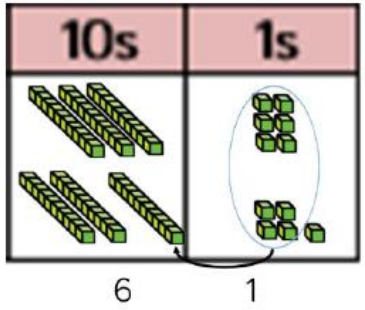
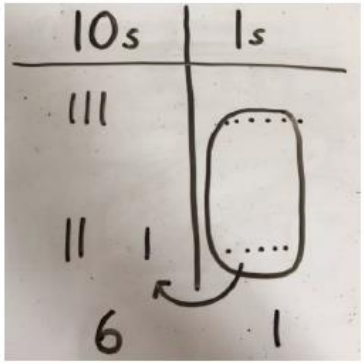
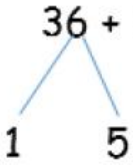
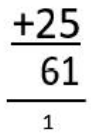
Key Language: Share, group, divide, divided by, half

Concrete	Pictorial	Abstract
Sharing using a range of objects. 6 ÷ 2 	Represent the sharing pictorially. 	6 ÷ 2 = 3  Children should also be encouraged to use their 2 times tables facts.
Repeated subtraction using Cuisenaire rods above a ruler. 6 ÷ 2  3 groups of 2	Children to represent repeated subtraction pictorially. 	Abstract number line to represent the equal groups that have been subtracted. 

Year 2

Addition:

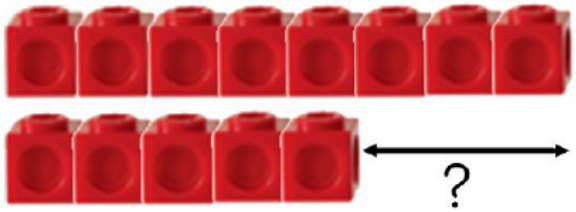
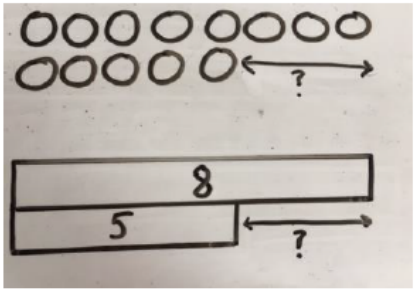
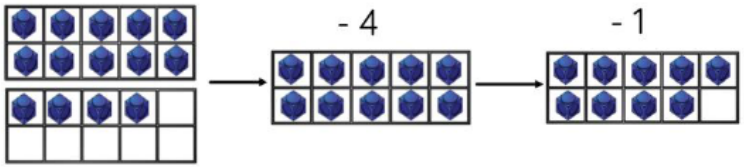
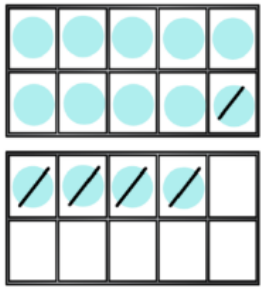
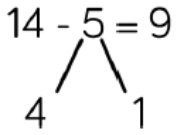
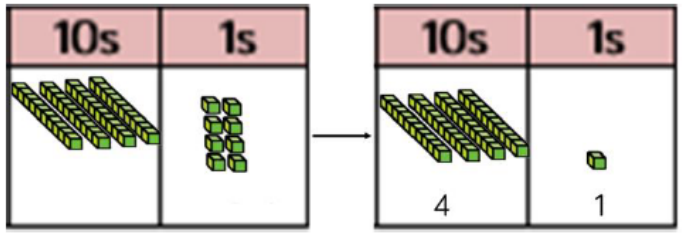
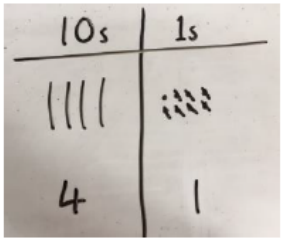
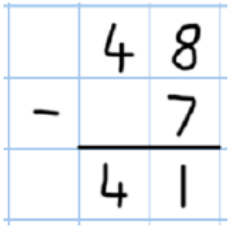
Key Language: Sum, total, parts and whole, plus, add, altogether, more, ‘is equal to’, ‘is the same as’.

TO + O using base 10. Continue to develop understanding of partitioning and place value. 41 + 8 	Children to represent the base 10 e.g. lines for tens and dot/crosses for ones. 	41 + 8  1 + 8 = 9 40 + 9 = 49 
TO + TO using base 10. Continue to develop understanding of partitioning and place value. 36 + 25 	Chidlren to represent the base 10 in a place value chart. 	Looking for ways to make 10.  30 + 20 = 50 5 + 5 = 10 50 + 10 + 1 = 61 Formal method: 

Year 2

Subtraction: (Formal algorithm at GDS)

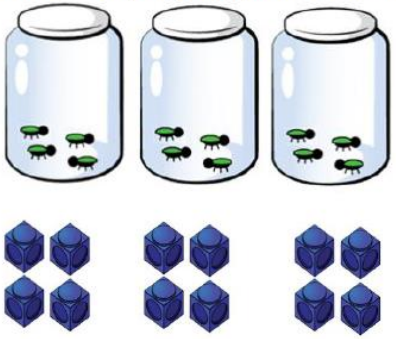
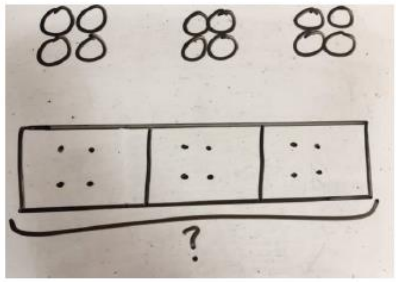
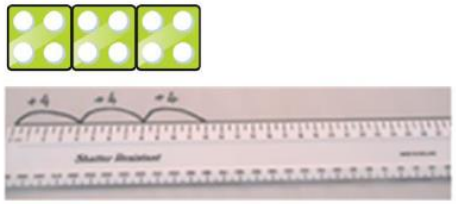
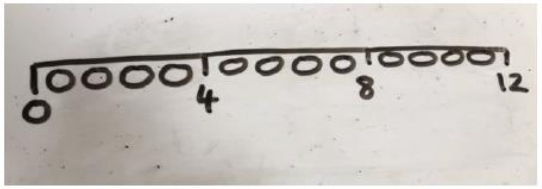
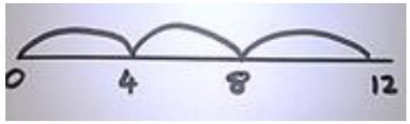
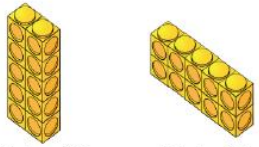
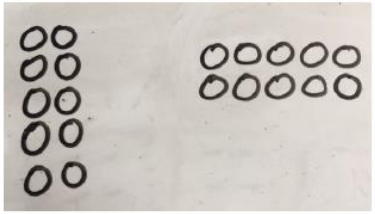
Key Language: Take away, less than, the difference, subtract, minus, fewer, decrease

Finding the difference (using cubes, Numicon or Cuisenaire rods, other objects can also be used). Calculate the difference between 8 and 5. 	Children to draw the cubes/other concrete objects which they have used or use the bar model to illustrate what they need to calculate. 	Find the difference between 8 and 5. 8 – 5, the difference is ☐ Children to explore why 9 - 6 = 8 – 5 = 7 – 4 have the same difference.
Making 10 using ten frames. 14 – 5 	Children to present the ten frame pictorially and discuss what they did to make 10. 	Children to show how they can make 10 by partitioning the subtrahend.  14 – 4 = 10 10 – 1 = 9
Column method using base 10. 48-7 	Children to represent the base 10 pictorially. 	Column method or children could count back 7. 

Year 2

Multiplication:

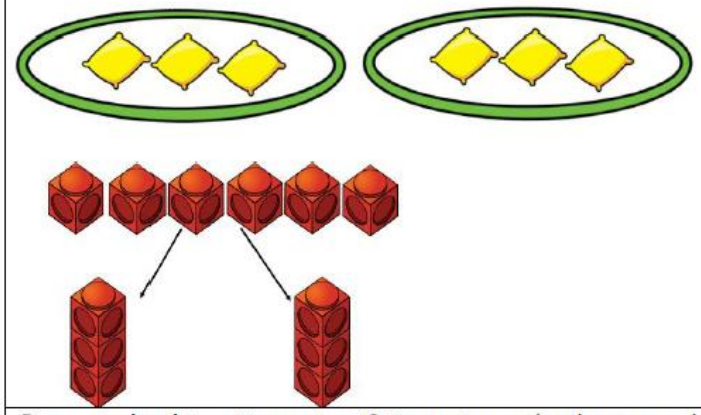
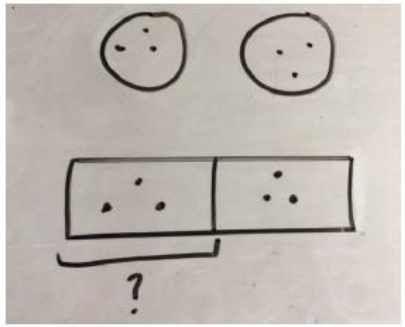
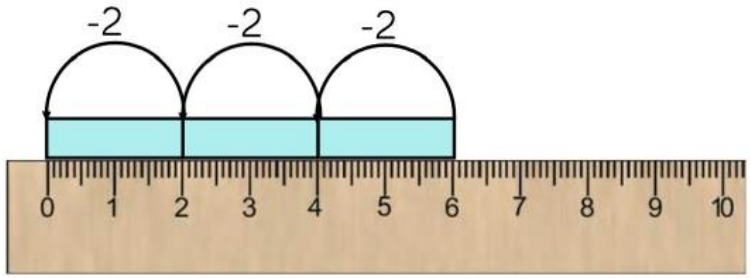
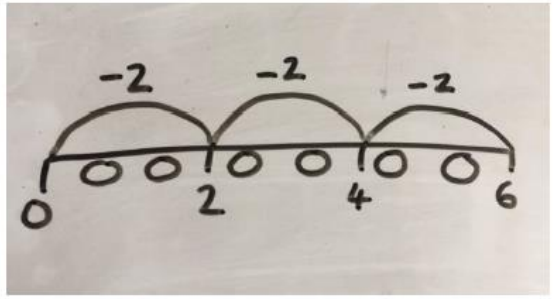
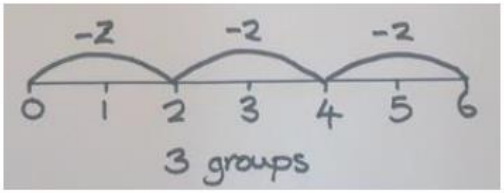
Key Language: Double, times, multiplied by, the product of, groups of, lots of, equal groups

Concrete	Pictorial	Abstract
Repeated grouping/repeated addition 3 × 4 4 + 4 + 4 There are 3 equal groups, with 4 in each group. 	Children to represent the practical resources in a picture and use a bar model. 	3 × 4 = 12 4 + 4 + 4 = 12
Number lines to show repeated groups- 3 × 4  Cuisenaire rods can be used too.	Represent this pictorially alongside a number line e.g.: 	Abstract number line showing three jumps of four. 3 × 4 = 12 
Use arrays to illustrate commutativity counters and other objects can also be used. 2 × 5 = 5 × 2  2 lots of 5 5 lots of 2	Children to represent the arrays pictorially. 	Children to be able to use an array to write a range of calculations e.g. 10 = 2 × 5 5 × 2 = 10 2 + 2 + 2 + 2 + 2 = 10 10 = 5 + 5

Year 2

Division:

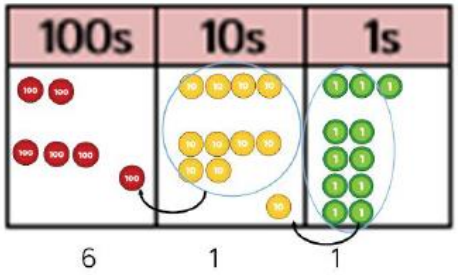
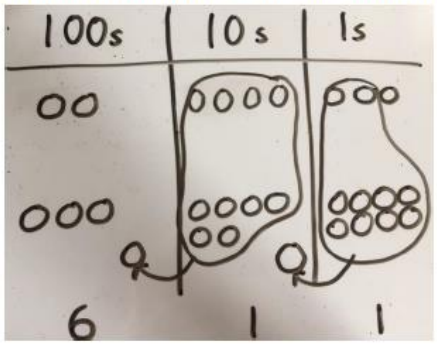
Key Language: Share, group, divide, divided by, half

Concrete	Pictorial	Abstract
Sharing using a range of objects. 6 ÷ 2 	Represent the sharing pictorially. 	6 ÷ 2 = 3  Children should also be encouraged to use their 2 times tables facts.
Repeated subtraction using Cuisenaire rods above a ruler. 6 ÷ 2  3 groups of 2	Children to represent repeated subtraction pictorially. 	Abstract number line to represent the equal groups that have been subtracted. 

Year 3

Addition: Introduce exchanges. 3d + 3d

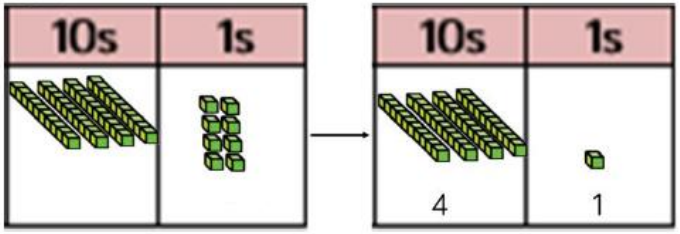
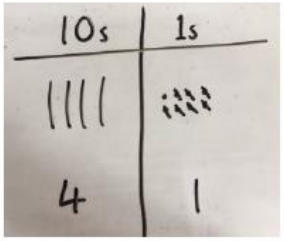
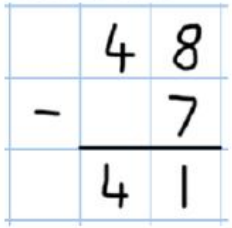
Key Language: Sum, total, parts and whole, plus, add, altogether, more, 'is equal to', 'is the same as'.

Use of place value counters to add HTO + TO, HTO + HTO etc. When there are 10 ones in the 1s column- we exchange for 1 ten, when there are 10 tens in the 10s column- we exchange for 1 hundred.  	Chidren to represent the counters in a place value chart, circling when they make an exchange.  	243 +368 611 1 1

Year 3

Subtraction:

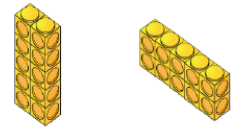
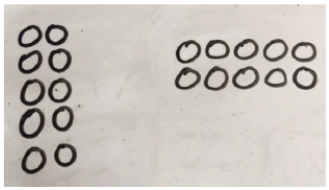
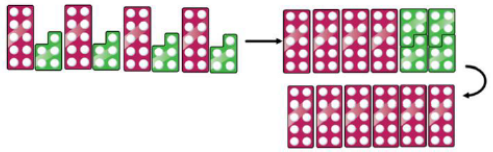
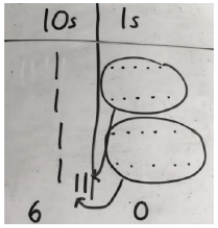
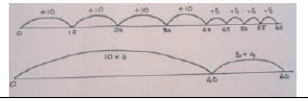
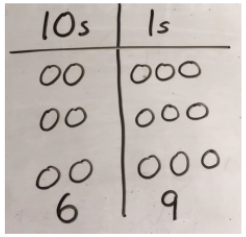
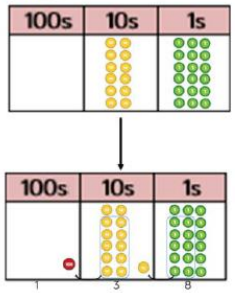
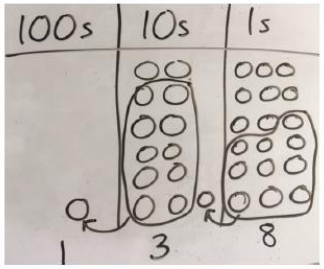
Key Language: Take away, less than, the difference, subtract, minus, fewer, decrease

Column method using base 10. 48-7  	Children to represent the base 10 pictorially.  	Column method or children could count back 7. 

Year 3

Multiplication: (x2,3,4,5,8,10)

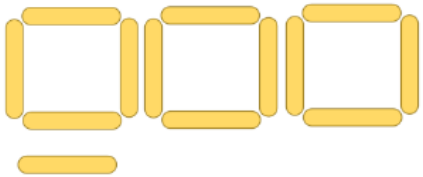
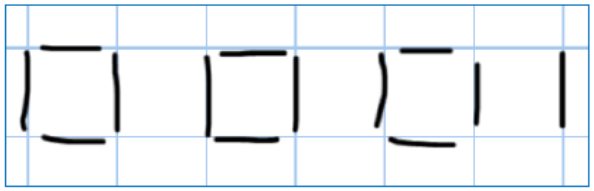
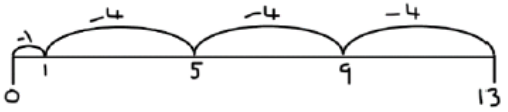
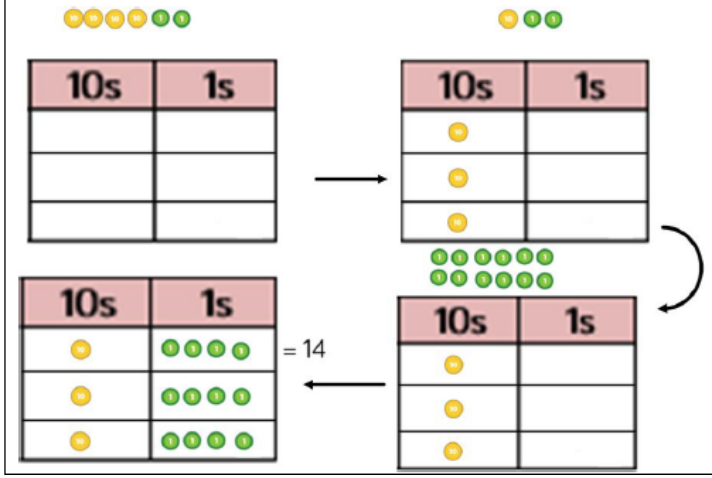
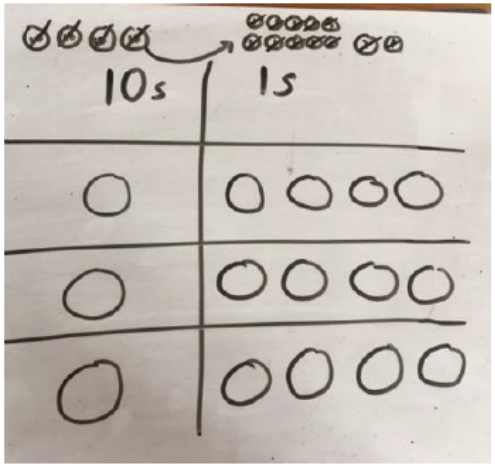
Key Language: Double, times, multiplied by, the product of, groups of, lots of, equal groups

Use arrays to illustrate commutativity counters and other objects can also be used. $2 \times 5 = 5 \times 2$  2 lots of 5 5 lots of 2	Children to represent the arrays pictorially. 	Children to be able to use an array to write a range of calculations e.g. $10 = 2 \times 5$ $5 \times 2 = 10$ $2 + 2 + 2 + 2 + 2 = 10$ $10 = 5 + 5$
Partition to multiply using Numicon, base 10 or Cuisenaire rods. 4×15 	Children to represent the concrete manipulatives pictorially. 	Children to be encouraged to show the steps they have taken. 4 x 15 10 5 10 x 4 = 40 5 x 4 = 20 40 + 20 = 60 A number line can also be used 
Formal column method with place value counters (base 10 can also be used.) 3×23 	Children to represent the counters pictorially. 	Children to record what it is they are doing to show understanding. 3×23 $3 \times 20 = 60$ $3 \times 3 = 9$ 20 3 $60 + 9 = 69$ 23 × 3 69
Formal column method with place value counters. 6 x 23 	Children to represent the counters/base 10, pictorially e.g. the image below. 	Formal written method 6 x 23 = 23 × 6 138 1 1

Year 3

Division: (÷2,3,4,5,8,10)

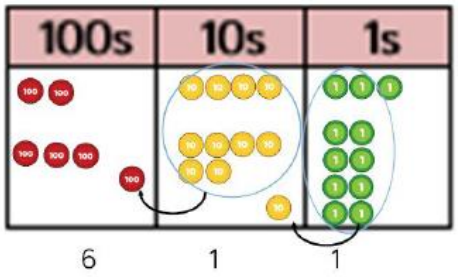
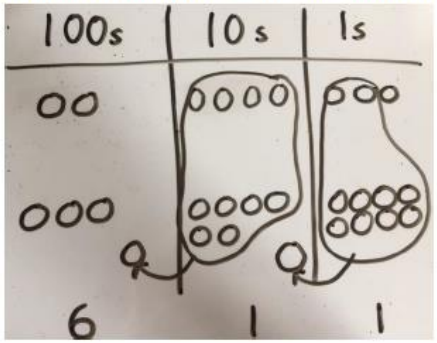
Key Language: Share, group, divide, divided by, half

2d ÷ 1d with remainders using lollipop sticks. Cuisenaire rods, above a ruler can also be used. 13 ÷ 4 Use of lollipop sticks to form wholes- squares are made because we are dividing by 4.  There are 3 whole squares, with 1 left over.	Children to represent the lollipop sticks pictorially.  There are 3 whole squares, with 1 left over.	13 ÷ 4 = 3 remainder 1 Children should be encouraged to use their times table facts; they could also represent repeated addition on a number line. '3 groups of 4, with 1 left over' 
Sharing using place value counters. 42 ÷ 3 = 14 	Children to represent the place value counters pictorially. 	Children to be able to make sense of the place value counters and write calculations to show the process. 42 ÷ 3 42 = 30 + 12 30 ÷ 3 = 10 12 ÷ 3 = 4 10 + 4 = 14

Year 4

Addition: up to 4d to include decimals

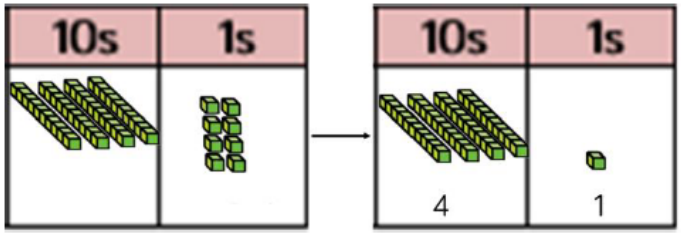
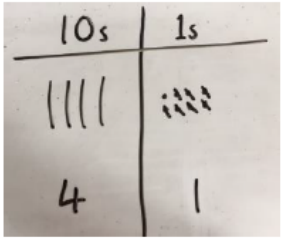
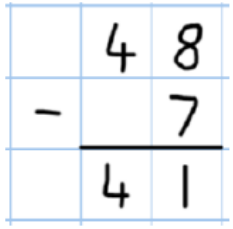
Key Language: Sum, total, parts and whole, plus, add, altogether, more, 'is equal to', 'is the same as'.

Use of place value counters to add HTO + TO, HTO + HTO etc. When there are 10 ones in the 1s column- we exchange for 1 ten, when there are 10 tens in the 10s column- we exchange for 1 hundred. 	Chidren to represent the counters in a place value chart, circling when they make an exchange. 	243 +368 611 1 1

Year 4

Subtraction: 4d – 4d including 2dp

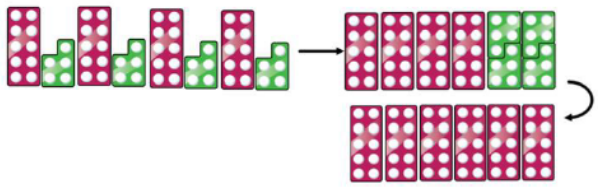
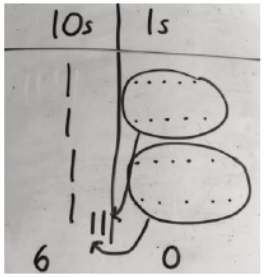
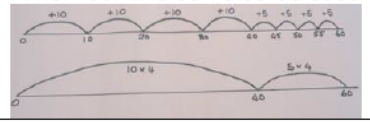
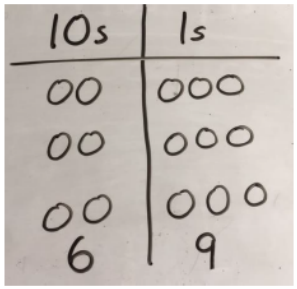
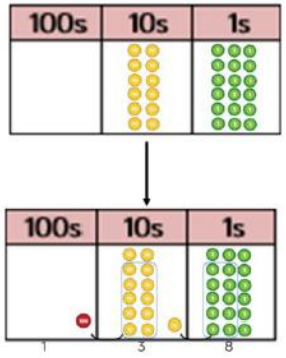
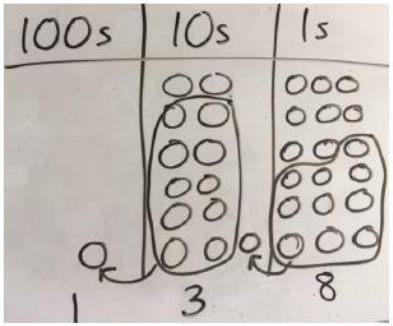
Key Language: Take away, less than, the difference, subtract, minus, fewer, decrease

Column method using base 10. 48-7 	Children to represent the base 10 pictorially. 	Column method or children could count back 7. 

Year 4

Multiplication: (all times-tables) 4d x 1d

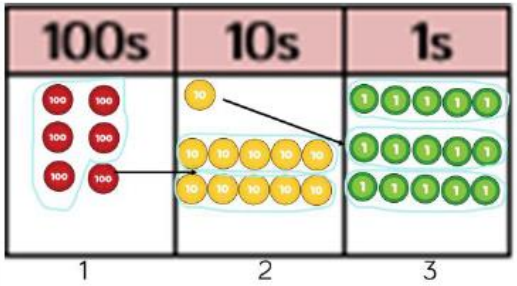
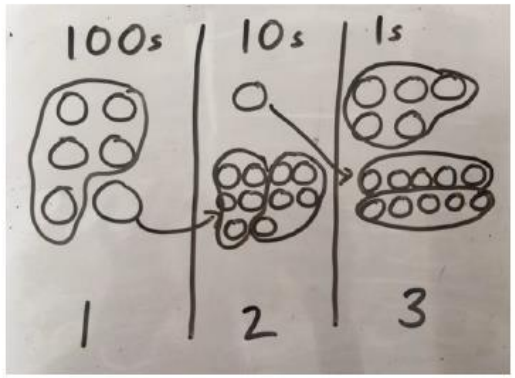
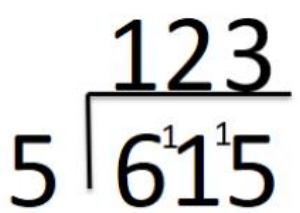
Key Language: Double, times, multiplied by, the product of, groups of, lots of, equal groups

Partition to multiply using Numicon, base 10 or Cuisenaire rods. 4 x 15 	Children to represent the concrete manipulatives pictorially. 	Children to be encouraged to show the steps they have taken. 4 x 15 10 5 10 x 4 = 40 5 x 4 = 20 40 + 20 = 60 A number line can also be used 
Formal column method with place value counters (base 10 can also be used.) 3 x 23 	Children to represent the counters pictorially. 	Children to record what it is they are doing to show understanding. 3 x 23 20 3 3 x 20 = 60 3 x 3 = 9 60 + 9 = 69 23 x 3 69
Formal column method with place value counters. 6 x 23 	Children to represent the counters/base 10, pictorially e.g. the image below. 	Formal written method 6 x 23 = 23 x 6 138 1 1

Year 4

Division: (all divisors) 4d÷1d incl remainders

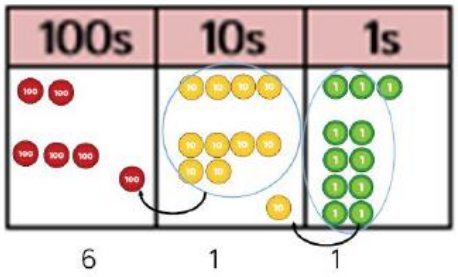
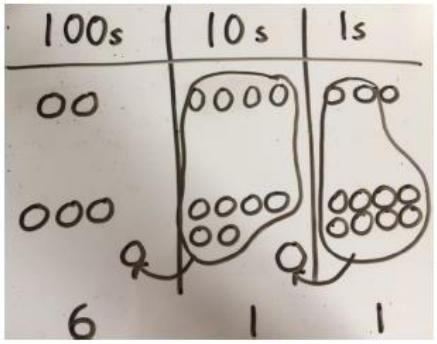
Key Language: Share, group, divide, divided by, half

Short division using place value counters to group. 615 ÷ 5  1. Make 615 with place value counters. 2. How many groups of 5 hundreds can you make with 6 hundred counters? 3. Exchange 1 hundred for 10 tens. 4. How many groups of 5 tens can you make with 11 ten counters? 5. Exchange 1 ten for 10 ones. 6. How many groups of 5 ones can you make with 15 ones?	Represent the place value counters pictorially.  	Children to the calculation using the short division scaffold. 

Year 5

Addition: Up to 4 or more digits and decimals to 3dp

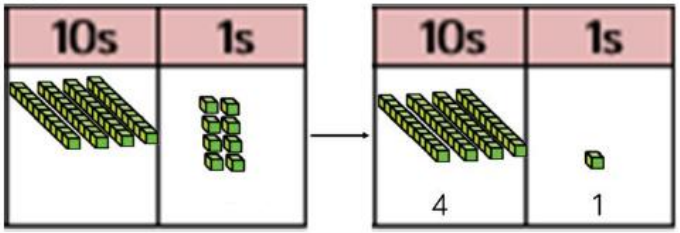
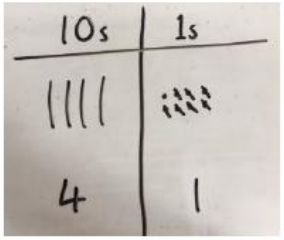
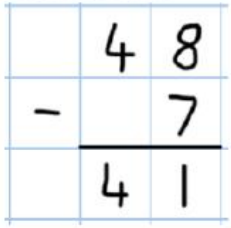
Key Language: Sum, total, parts and whole, plus, add, altogether, more, 'is equal to', 'is the same as'.

Use of place value counters to add HTO + TO, HTO + HTO etc. When there are 10 ones in the 1s column- we exchange for 1 ten, when there are 10 tens in the 10s column- we exchange for 1 hundred. 	Chidren to represent the counters in a place value chart, circling when they make an exchange. 	243 +368 611 1 1

Year 5

Subtraction: 4d – 4d inc 3dp

Key Language: Take away, less than, the difference, subtract, minus, fewer, decrease

Column method using base 10. 48-7 	Children to represent the base 10 pictorially. 	Column method or children could count back 7. 

Year 5

Multiplication: (all times tables) 4d x 2d

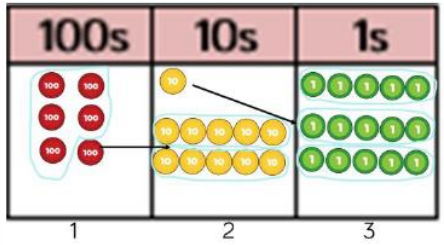
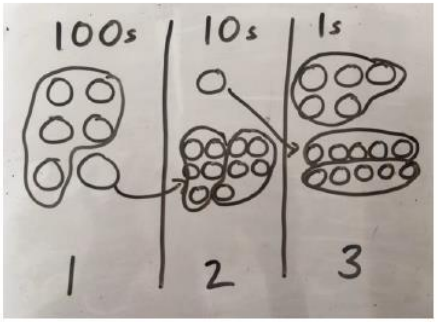
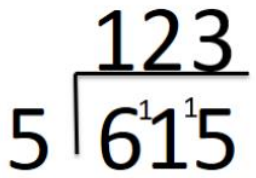
When children start to multiply 3d × 3d and 4d × 2d etc., they should be confident with the abstract: To get 744 children have solved 6 × 124. To get 2480 they have solved 20 × 124.	124 × 26 744 (6 × 124) 2480 (20 × 124) 3224 Answer: 3224

Key Language: Double, times, multiplied by, the product of, groups of, lots of, equal groups

Year 5

Division:

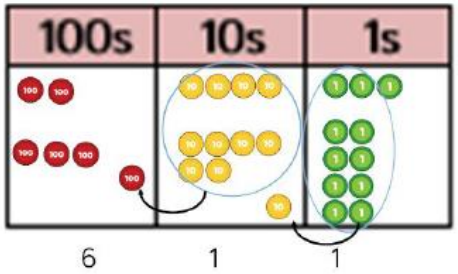
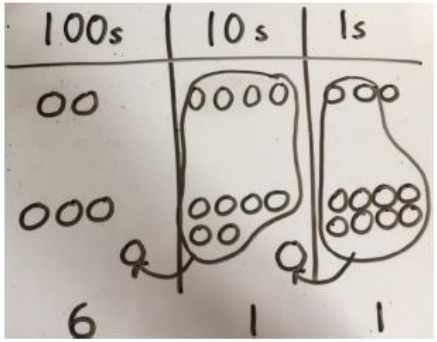
Key Language: Share, group, divide, divided by, half

Short division using place value counters to group. 615 ÷ 5  1. Make 615 with place value counters. 2. How many groups of 5 hundreds can you make with 6 hundred counters? 3. Exchange 1 hundred for 10 tens. 4. How many groups of 5 tens can you make with 11 ten counters? 5. Exchange 1 ten for 10 ones. 6. How many groups of 5 ones can you make with 15 ones?	Represent the place value counters pictorially.  	Children to the calculation using the short division scaffold. 

Year 6

Addition: Any number of digits including decimals to 3dp

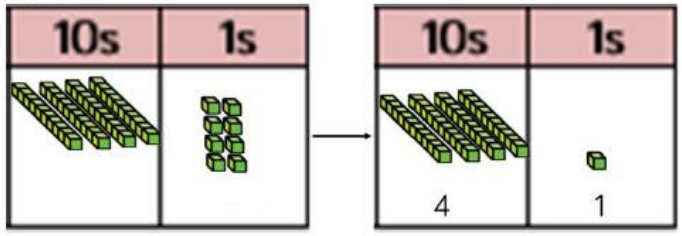
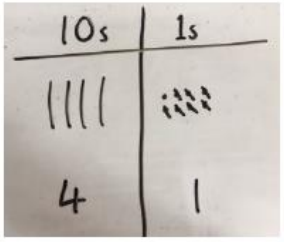
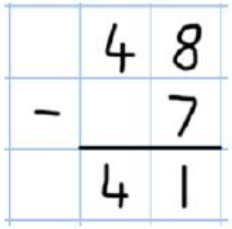
Key Language: Sum, total, parts and whole, plus, add, altogether, more, 'is equal to', 'is the same as'.

Use of place value counters to add HTO + TO, HTO + HTO etc. When there are 10 ones in the 1s column- we exchange for 1 ten, when there are 10 tens in the 10s column- we exchange for 1 hundred. 	Chidren to represent the counters in a place value chart, circling when they make an exchange. 	$\begin{array}{r} 243 \\ +368 \\ \hline 611 \\ \hline 1\ 1 \end{array}$

Year 6

Subtraction: Any number of digits including decimals to 3dp

Key Language: Take away, less than, the difference, subtract, minus, fewer, decrease

Column method using base 10. 48-7 	Children to represent the base 10 pictorially. 	Column method or children could count back 7. 

Year 6

Multiplication: (all times tables) 4d x 2d

Key Language: Double, times, multiplied by, the product of, groups of, lots of, equal groups

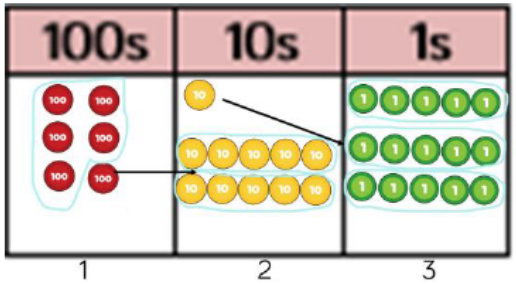
When children start to multiply 3d × 3d and 4d × 2d etc., they should be confident with the abstract: To get 744 children have solved 6 × 124. To get 2480 they have solved 20 × 124.	 Answer: 3224

Year 6

Division:

Key Language: Share, group, divide, divided by, half

Short division using place value counters to group.
615 ÷ 5



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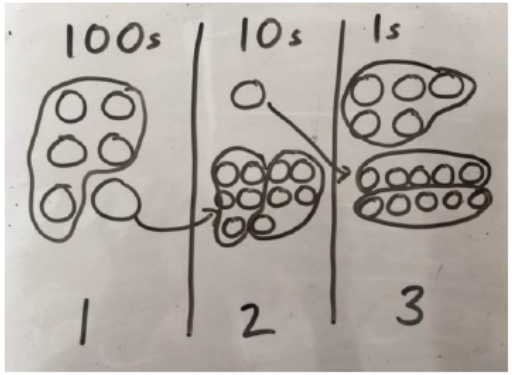
4. How many groups of 5 tens can you make with 11 ten counters?
5. Exchange 1 ten for 10 ones.
6. How many groups of 5 ones can you make with 15 ones?

Represent the place value counters pictorially.

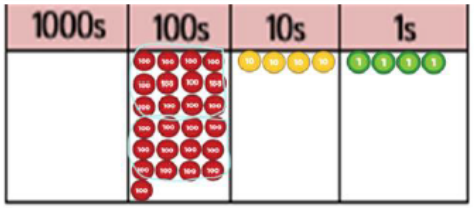


Children to the calculation using the short division scaffold.

$$5\overline{)615}$$

Long division using place value counters
2544 ÷ 12

We can't group 2 thousands into groups of 12 so will exchange them.



We can group 24 hundreds into groups of 12 which leaves with 1 hundred.

$$\begin{array}{r} 02 \\ 12\overline{)2544} \\ \underline{24} \\ 1 \end{array}$$